Cylindrical Coordinates:

$$x = r \cos\theta$$
, $y = r \sin\theta$, $z = z$, $r = \sqrt{x^2 + y^2}$, $dV = r dz dr d\theta$

Spherical Coordinates:

$$x = \rho \sin \varphi \cos \theta, \ y = \rho \sin \varphi \sin \theta, \ z = \rho \cos \varphi, \quad \rho = \sqrt{x^2 + y^2 + z^2}, \ dV = \rho^2 \sin \varphi \, d\rho d\varphi d\theta$$

Green's Theorem:

$$\int_{C} P(x,y)dx + Q(x,y)dy = \int_{D} \int \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y}\right) dA$$

Here C is a simple closed curve in the x-y plane with counterclockwise orientation and D is the region enclosed by C.

Surfaces Described by $\vec{r}(u, v)$:

$$dS = \left| \frac{\partial \vec{r}}{\partial u} \times \frac{\partial \vec{r}}{\partial v} \right| du dv, \quad \vec{n} dS = \pm \frac{\partial \vec{r}}{\partial u} \times \frac{\partial \vec{r}}{\partial v} du dv$$

Surfaces Described by z = f(x, y):

$$dS = \sqrt{1 + f_x^2 + f_y^2} \ dydx, \quad \vec{n}dS = \pm \left(f_x \vec{i} + f_y \vec{j} - \vec{k}\right) dydx$$

Sphere of Radius a > 0 Centered at (0,0,0):

$$\vec{r}(\varphi,\theta) = (a\sin\varphi\cos\theta)\vec{i} + (a\sin\varphi\sin\theta)\vec{j} + (a\cos\varphi)\vec{k} \ dS = a^2\sin\varphi d\varphi d\theta$$