

Partial Derivatives

Find f_{xx} , f_{xy} , f_{yx} , f_{yy}

1. $f(x, y) = x^2y + xy^2$

2. $f(x, y) = \frac{y + \tan(y)}{e^x}$

3. $f(x, y) = \ln(xy)$

4. $f(x, y) = \cos(x) \sin(y)$

Find the indicated partial derivative

5. $f(x, y) = x \cos(xy)$; $f_x(3, \pi)$

6. $f(x, y) = x^2\sqrt{x+y}$; $f_y(2, 7)$

7. $f(x, y) = \sin(y^3)$; $f_x(2, 1)$

8. $f(x, y) = x^y$; $f_y(3, 2)$

9. $f(x, y) = x^y$; $f_x(3, 2)$

Use Implicit Differentiation to find $\partial z/\partial x$ and $\partial z/\partial y$

10. $x^2 + y^2 = \sin(yz)$

11. $xe^y = zy$

12. $z + x = xyz$

13. $4x - \sin(z) = y^2z$

Tangent Planes

Find an equation of the tangent plane to the given surface at the specified point

14. $z = y^2 + 3x^2, (1, 2, 7)$

15. $z = \sin(x) \cos(y), (\pi, \pi, 0)$

16. $z = xe^y, (1, 0, 1)$

17. $z = \sqrt{y} \ln(x), (e, 4, 2)$

Anti-Derivatives (Not covered in class yet)

Find f given the partial derivatives.

18. $f_x(x, y) = -\frac{y}{2\sqrt{x^3}} + \frac{1}{2\sqrt{x}}$; $f_y(x, y) = \frac{1}{\sqrt{x}} + 1$

19. $f_x(x, y) = y \cos(xy) + \sin(y)$; $f_y(x, y) = (x+1) \cos y + x \cos(xy)$

20. $f_x(x, y) = \frac{1}{x} - \frac{1}{x^2 y}$; $f_y = -\frac{2}{y^3} - \frac{1}{xy^2}$

21. $f_x(x, y) = \sin^2(y)$; $f_y(x, y) = (x+1) \sin(2y)$