

1. The set of points  $(x, y, z)$  such that  $x - y + z = 0$  is
- a line
  - a plane
  - The empty set
  - hard to decipher

Determine whether the following lines are coinciding, parallel, intersecting, or skew using the direction vectors.

2.  $\begin{array}{ll} x = 1+t & x = 3 + \frac{t}{2} \\ y = 4-t & y = 4 - \frac{t}{2} \\ z = 2+2t & z = t - 6 \end{array}$

3.  $\begin{array}{ll} x = 3 & x = t \\ y = 6+t & y = 4-t \\ z = 4-t & z = 1+2t \end{array}$

4.  $\begin{array}{ll} x = 3t & x = 3-6t \\ y = 1+3t & y = 4-6t \\ z = 1-2t & z = -1+4t \end{array}$

5.  $\begin{array}{ll} x = 1+2t & x = 8+3t \\ y = -3+t & y = t \\ z = 2 & z = 4+2t \end{array}$

6. Let  $\vec{a} = \langle -3, 1, 2 \rangle$  and  $\vec{b} = \langle 0, 1, -1 \rangle$ . Find  $\vec{a} \times \vec{b}$  and verify that it is orthogonal to both  $\vec{a}$  and  $\vec{b}$

Use the right hand rule to find the following cross products.

7.  $\hat{i} \times \hat{k}$

10.  $\hat{j} \times \hat{k}$

8.  $\hat{k} \times (-\hat{j})$

11.  $(-\hat{i}) \times \hat{k}$

9.  $\hat{j} \times (-\hat{i})$

12.  $\hat{i} \times (-\hat{j})$

True or False

13.  $(\vec{a} \times \vec{b}) \times \vec{c} = \vec{a} \times (\vec{b} \times \vec{c})$

14.  $\vec{a} \times (\vec{b} + \vec{c}) = (\vec{a} \times \vec{b}) + (\vec{a} \times \vec{c})$

15.  $\vec{a} \times \vec{b} = \vec{b} \times \vec{a}$

16.  $(\vec{a} \times \vec{b}) \cdot \vec{c} = \vec{a} \cdot (\vec{b} \times \vec{c})$

17.  $(\vec{a} \cdot \vec{b}) \cdot \vec{c} = \vec{a} \cdot (\vec{b} \cdot \vec{c})$

18.  $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{a}$

19.  $\vec{a} \cdot (\vec{b} \times \vec{c}) = (\vec{a} \cdot \vec{b}) \times \vec{c}$

20.  $\vec{a} \times \vec{b} = -\vec{b} \times \vec{a}$

21. Consider a parallelopiped with adjacent edges  $\vec{PQ}$ ,  $\vec{PR}$ ,  $\vec{PS}$  where  $\vec{P} = \langle 0, 1, -1 \rangle$ ,  $\vec{Q} = \langle 2, -2, 0 \rangle$ ,  $\vec{R} = \langle 1, 2, 3 \rangle$ ,  $\vec{S} = \langle -1, -1, -1 \rangle$ . Find the area of the parallelopiped.

22. What vectors are perpendicular to the  $yz$ -plane?