

MATH 54 FALL 2017: DISCUSSION 205/208 QUIZ#6

GSI: CHRISTOPHER EUR, DATE: 10/6/2017

STUDENT NAME: _____

Problem 1. Let V be the vector space of 2×2 matrices. Let $L := \left\{ \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}, \begin{bmatrix} 0 & 0 \\ 1 & 0 \end{bmatrix}, \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} \right\}$ be a list of vectors in V .

(a) (2 points) Extend L to a basis B of V (you need not justify B you create is a basis).

(b) (3 points) Write the coordinates of $\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ with respect of B you created in part (a).

Problem 2. (5 points) Let $\mathbb{P}_1 := \{a_0 + a_1t : a_0, a_1 \in \mathbb{R}\}$ be the vector space of polynomials of degree ≤ 1 . Find all values of $c \in \mathbb{R}$ for which $\{1 + t, 1 + ct\}$ is a basis for \mathbb{P}_1 (with justification)