

MATH 54 FALL 2017: DISCUSSION 205/208 QUIZ#13

GSI: CHRISTOPHER EUR, DATE: 12/1/2017

STUDENT NAME: _____

Problem 1. (5 points) Solve for $u(x, t)$ where $-\pi < x < \pi$ and $t > 0$ satisfying the following (wave) equation:

$$\begin{aligned}4u_{xx} &= u_{tt} \\ u(-\pi, t) &= u(\pi, t) = 0 \quad \forall t > 0 \\ u(x, 0) &= \sin 3x + 4 \sin 5x \\ u_t(x, 0) &= 2 \cos 4x\end{aligned}$$

Problem 2. (5 points) Solve for $u(x, t)$ where $-\frac{\pi}{2} < x < \frac{\pi}{2}$ and $t > 0$ satisfying the following (heat) equation:

$$\begin{aligned}5u_{xx} &= u_t \\ u(-\pi, t) &= u(\pi, t), \quad u_x(-\pi, t) = u_x(\pi, t) \quad \forall t > 0 \text{ (CAREFUL HERE!)} \\ u(x, 0) &= 3 \sin 2x + 5 \cos 6x\end{aligned}$$