

**MATH 54 FALL 2016: DISCUSSION 102/105 QUIZ#12**

GSI: CHRISTOPHER EUR, DATE: 11/21/2016

STUDENT NAME: \_\_\_\_\_

*Problem 1.* Consider the linear differential operator  $\ell(y) := y'' + 2y' + y$ . Find the general solution to  $\ell(y) = t \cos t$  as follows:

(a) (2 points) Find  $\ker \ell$ .

(b) (3 points) Find a particular solution to  $\ell(y) = t \cos t$  (Hint: you might end up writing down a  $4 \times 4$  matrix).

(c) (1 point) Using the previous two parts, state what the general solution to  $\ell(y) = t \cos t$  is.

*Problem 2.* (4 points) Find a particular solution to  $y'' - 3y' + 2y = e^{2t}$ .