Directed Ramsey number for trees

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Given an oriented graph H, the k-colour oriented Ramsey number of H, denoted by $\overrightarrow{R}(H,k)$, is the least integer n, for which every k-edge-coloured tournament on n vertices contains a monochromatic copy of H. We show that $\overrightarrow{R}(T,k) \leq c_k |T|^k$ for any oriented tree T, which, in general, is tight up to a constant factor. We also obtain a stronger bound, when H is an arbitrarily oriented path.