The Satisfiability Threshold for k-XORSAT

Gregory Sorkin (London School of Economics)

Abstract

We consider "unconstrained" random k-XORSAT, which is a uniformly random system of m linear non-homogeneous equations in \mathbb{F}_2 over n variables, each equation containing $k \geq 3$ variables, and also consider a "constrained" model where every variable appears in at least two equations. Dubois and Mandler proved that m/n = 1 is a sharp threshold for solvability of constrained 3-XORSAT, and analyzed the 2-core of a random 3-uniform hypergraph to extend this result to find the threshold for unconstrained 3-XORSAT. We show that m/n = 1 remains a sharp threshold for solvability of constrained k-XORSAT for every $k \geq 3$, and we use Molloy's analysis of the 2-core of a random k-uniform hypergraph to extend this result to find the threshold for unconstrained k-XORSAT.

This is joint work with Boris Pittel.