Problem. A circle is growing with a radius increasing at a rate of 3 cm/s. Find a function (of the radius r) that gives the rate of change of the area of the circle.

Solution. The area of a circle is given by $A = \pi r^2$. Therefore, differentiating both sides with respect to t we get

$$\frac{dA}{dt} = 2\pi r \cdot \frac{dr}{dt}$$

We are given that $\frac{dr}{dt} = 3 \text{ cm/s}$. By substituting this in we get

$$\frac{dA}{dt} = 6\pi r$$